

Sort out the following notation and prove each of the expressions. Also describe each term/formula in English language.

- ${}_t p_x + {}_t q_x = 1$

- ${}_u | {}_t q_x = {}_u p_x - {}_{u+t} p_x$

- ${}_{t+u} p_x = {}_t p_x {}_u p_{x+t}$

- $\mu_x = -\frac{\frac{d}{dx} x p_0}{x p_0}$  and similarly  $\mu_{x+t} = -\frac{\frac{d}{dt} t p_x}{t p_x}$

- ${}_t p_x = e^{-\int_0^t \mu_{x+s} ds}$

- ${}_t q_x = \int_0^t {}_s p_x \mu_{x+s} ds$