

Learning the Language of the Universe: How to Study Math

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Effective
and
Efficient
Learning

“Efficiency is doing
things right;
effectiveness is doing
the right things.”

Peter Drucker

Traditional Method

- review the lesson, watch the video, etc.
- look over the examples worked in the text (only if you know mom/dad/teacher is going to ask)
- do homework problems (as quickly as humanly possible)
- repeat for several lessons
- maybe try some sort of chapter review/chapter test (if you're an over-achiever),
- take a test (usually with questions almost identical to the homework)

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Result:

- if you “get” math: success (ish)
- if you don't: utter frustration, doom, gloom, and despair
... then repeat with the advice to spend more time or do more problems

Better Solution
... but first



Adjust
Expectations
for your
student

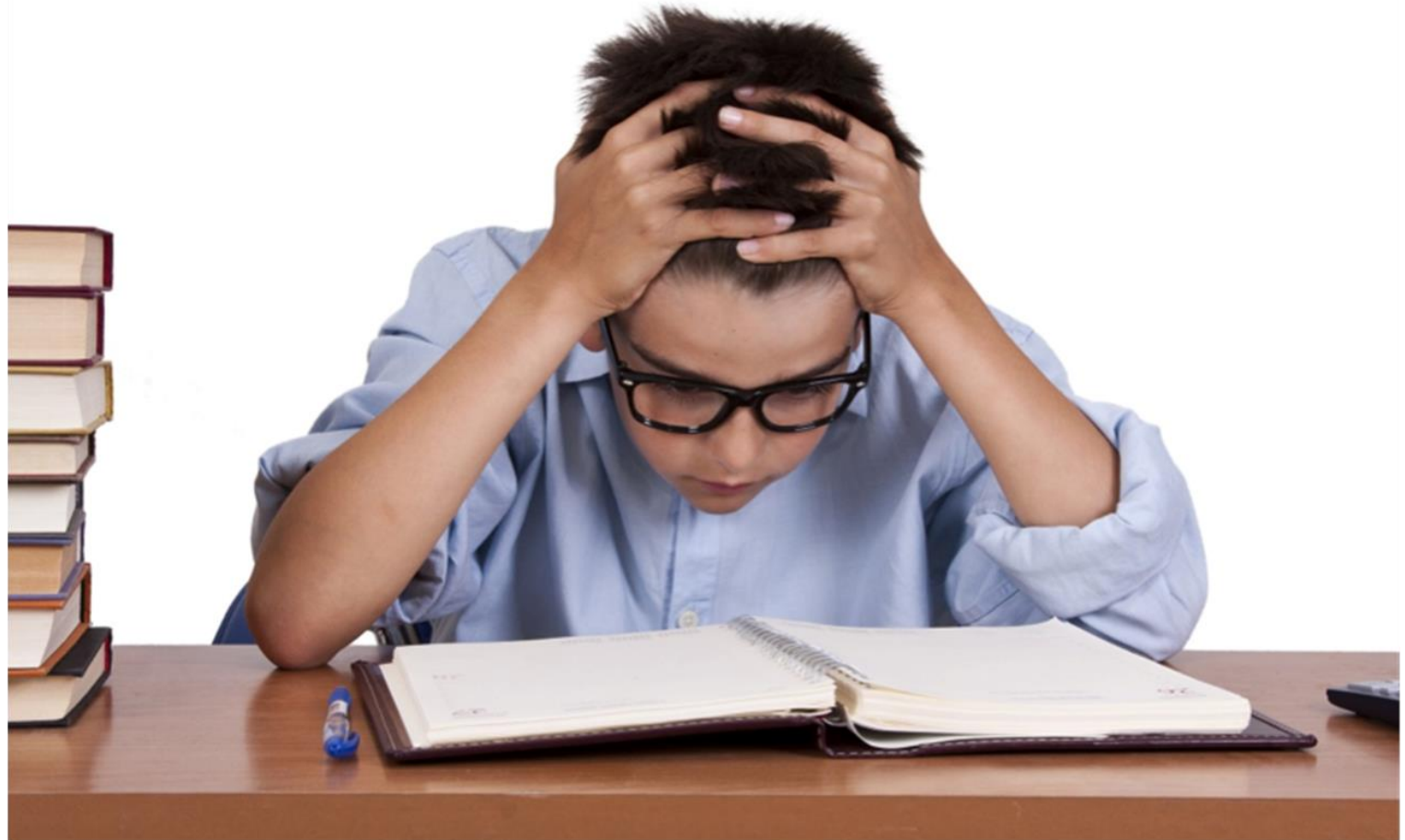
learning is hard
work



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Adjust Expectations for your student

learning takes focus



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Adjust Expectations for your student

learning is a skill



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Adjust Expectations for your student

mastery not
completion



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Adjust Expectations for you

prepare for
resistance



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Adjust Expectations for you

prepare for
resistance



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Adjust Expectations for you

rehearse your goals



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Adjust Expectations for you

improvement not
perfection



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Acknowledge
the balance ...



The Dream



Reality

Study
Effectively

means doing
the right stuff

Understand what math is and is not ...

- it is a process by which a variety of problems are solved
- it is not a numerical answer

Traditions are
great for a
reason ...



Some
traditions can
be improved
on ...

learn
effectively

Consider

- read/watch – but with a new purpose
- create study notes (1/2 to 1 page per topic)
- work problems (possibly not as many)
- have an oral quiz/teaching session
- take a test (recommend timed, speed and accuracy both matter)

Meet the goal:

learning a variety of processes by which many problems can be solved

Being effective

Adjust
Expectations

listen/read to
understand not
finish



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Being effective

Adjust
Expectations

describe
ideas/processes
in "English"

LONG DIVISION

- 1) Ask - how many times does the "divided by" go into the "first" number evenly (okay if there are some left over)
 - 2) write the "whole" number on top over the "first" number
 - 3) multiply "whole" number by "divided by" number and write under "first" number
 - 4) subtract and bring down "next" number to make new "first" number
 - 5) repeat until you run out
- * then write remainder (stuff left over)

other way to say it

$$3784 \text{ divided by } 16 = \frac{3784}{16}$$

OR

$$\begin{array}{r} 236 \text{ R}8 \\ 16 \overline{) 3784} \\ \underline{32} \\ 58 \\ \underline{48} \\ 104 \\ \underline{96} \\ 8 \end{array}$$

OR

$$236 \frac{8}{16} = 236 \frac{1}{2}$$

means
if divide 3784
into groups of 16
then you will
have 236 "full"
groups and
8 left over
(or $\frac{8}{16} = \frac{1}{2}$ of a group)



Being effective

Adjust
Expectations

work problems for
accuracy and speed

$$4 \overline{)236}$$

$$5 \overline{)165}$$

$$7 \overline{)518}$$

$$6 \overline{)516}$$

$$8 \overline{)448}$$

$$8 \overline{)720}$$

$$8 \overline{)304}$$

$$9 \overline{)774}$$

$$3 \overline{)162}$$

$$5 \overline{)285}$$

$$4 \overline{)244}$$

$$9 \overline{)765}$$

$$8 \overline{)480}$$

$$8 \overline{)192}$$

$$2 \overline{)76}$$



Being effective

Adjust Expectations

build
understanding
for the future

$$\begin{array}{r} 2x^2 + 5x - 7 \\ 3x - 2 \overline{) 6x^3 + 11x^2 - 31x + 1} \\ \underline{-(6x^3 - 4x^2)} \\ 15x^2 - 31x \\ \underline{-(15x^2 + 10x)} \\ 21x + 15 \\ \underline{-(-21x + 14)} \\ 1 \end{array}$$

$6x^3$ divided by $3x$ is $2x^2$.

Multiply $x + 2$ by $2x^2$.

Subtract. Bring down the next term. $15x^2$ divided by $3x$ is $5x$.

Multiply $3x - 2$ by $5x$.

Subtract. Bring down the next term. $-21x$ divided by $3x$ is -7 .

Multiply $3x - 2$ by -7 .

Subtract. The remainder is 1.

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Math Study Notes ...

create $\frac{1}{2}$ to 1 page notes for each lesson

check to see if they're any good

LONG DIVISION

- 1) ASK - how many times does the "divided by" go into the "first" number evenly (okay if there are some left over)
 - 2) write the "whole" number on top over the "first" number
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$$\text{OR} \quad 236 \frac{8}{16} = 236 \frac{1}{2}$$

$$\begin{array}{r} 58 \\ -16 \\ \hline 42 \\ -16 \\ \hline 26 \\ -16 \\ \hline 10 \end{array}$$

$$16 \times 96 = 1536$$

means
if divide 3784
into groups of 16
then you will
have 236 "full"
groups and
8 left over
(or $\frac{8}{16} = \frac{1}{2}$ of a group)

“Help” our
student learn
to use their
good study
notes?



“Helping”
without
diminishing
learning

embrace the
struggle,
build perseverance



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“Helping”
without
diminishing
learning

value mistakes,
build resilience

Explain how you regrouped
to solve the problem.

I USED my
brain

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“Helping”
without
diminishing
learning

answer questions
with questions



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Study Efficiently

means not being
stuck doing
something longer
than necessary



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Study Efficiently

math needs
good focus

Count “quality hours” not clock hours

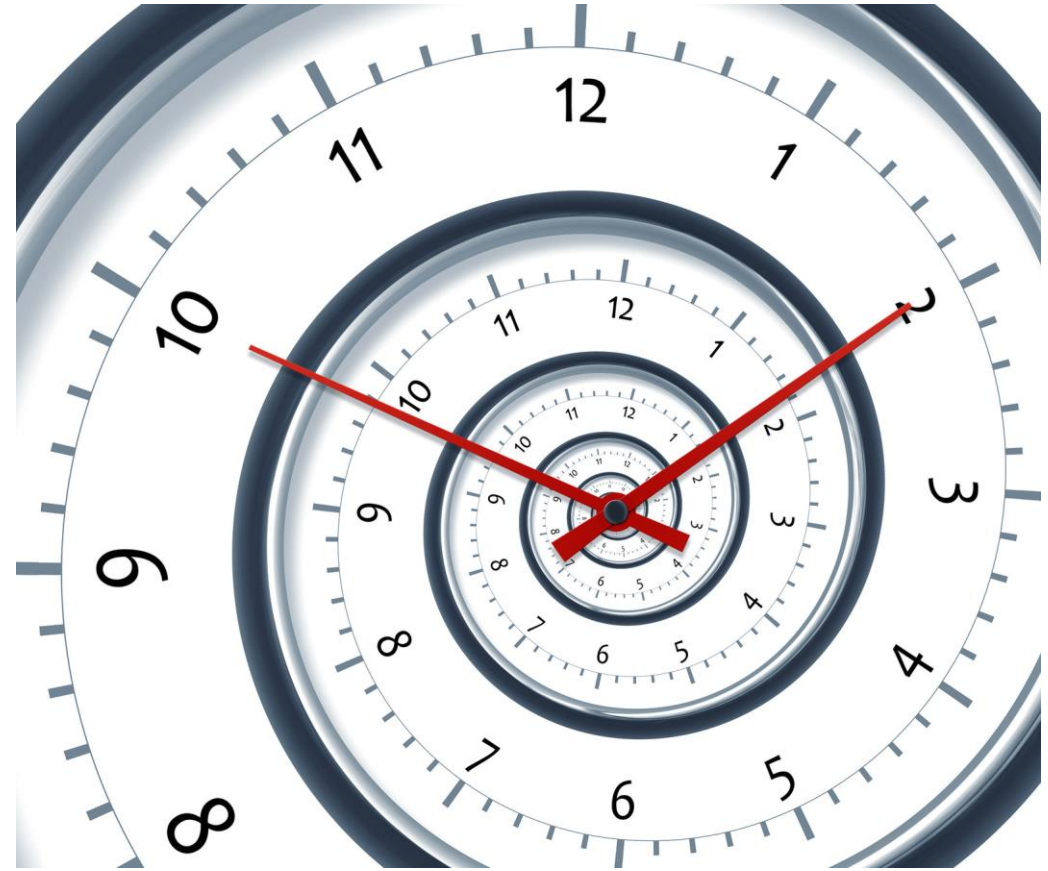
quality hours = clock hours * % of concentration



Study Efficiently

learn to get more
done in less time

Develop comfort with a time-pressured environment



Study Efficiently

don't let the
"opportunity" to
learn it "again"
slow you down

Learn it the first time:

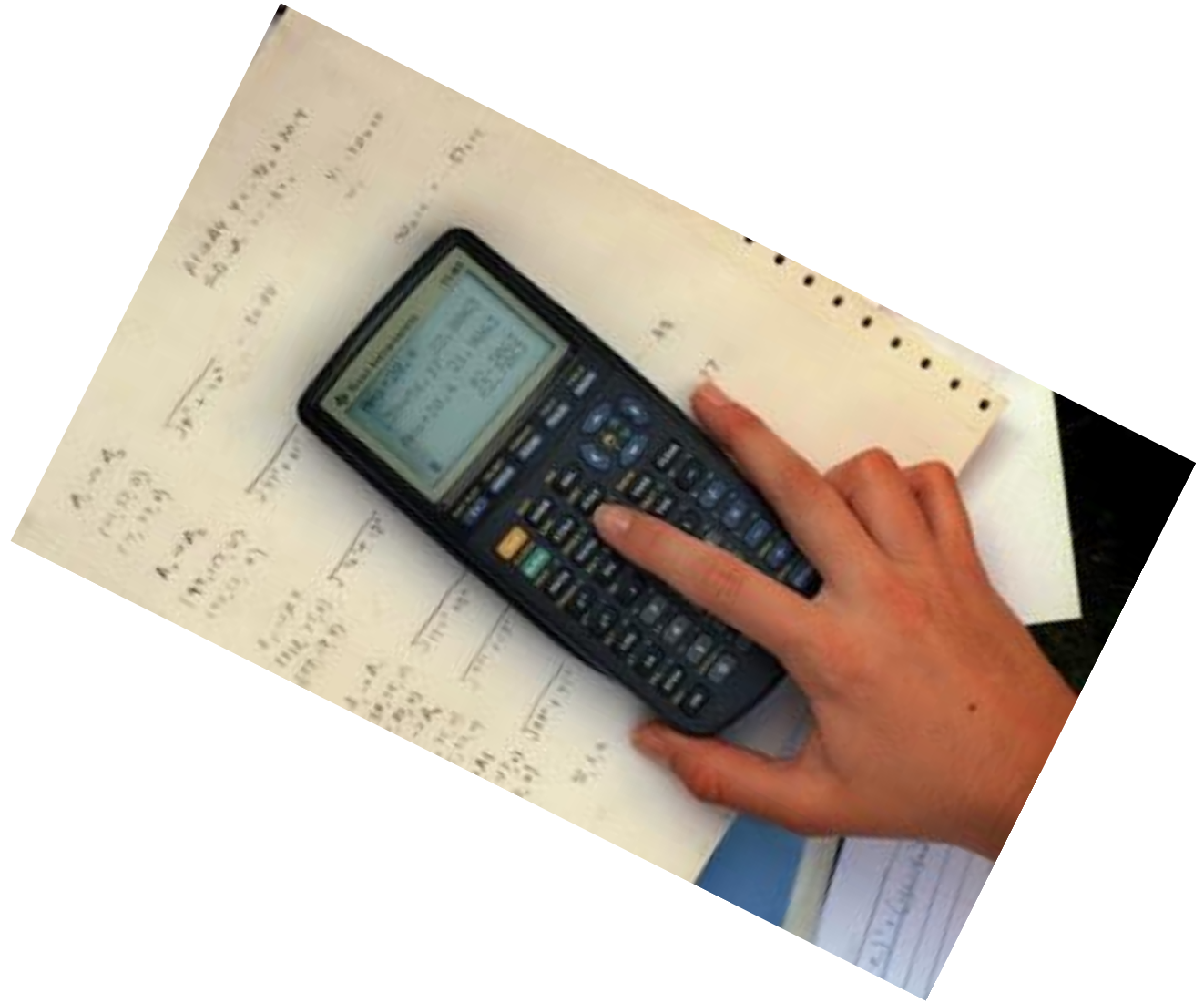
- Hide the solutions
- Sorry, no redos allowed
- Cheat sheets are verboten



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Study Efficiently

break free
from bondage
to calculators



Study Efficiently

develop more than
one skill at a time

Develop critical reading/writing
and communication

- describe the problems?
- how to solve?
- teach it to someone else?



Allocate your math time well

.... fast is slow,
so don't rush to get
problems done

Before “starting the homework”
... take 5 and test understanding

- explain in “normal English”
- ask, “how was I supposed to know?”
- pick a problem, and only do exactly what they say

Allocate your
math time well

use homework
problems
strategically



OR



Keep the
goal in mind

Mastery not
completion



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